

at has a constant direction

If ϕ represent the potential then the level surface are called equipotential

If ϕ " the temperature then the level surface isothermal

$$\nabla = \frac{\partial}{\partial x} \hat{i} + \frac{\partial}{\partial y} \hat{j} + \frac{\partial}{\partial z} \hat{k}$$

$$\text{grad } \phi = \nabla \phi = \frac{\partial \phi}{\partial x} \hat{i} + \frac{\partial \phi}{\partial y} \hat{j} + \frac{\partial \phi}{\partial z} \hat{k}$$

∇ is gradient, divergence and curl.
Gradient of a scalar function

$$\nabla \phi = \left(\frac{\partial}{\partial x} \hat{i} + \frac{\partial}{\partial y} \hat{j} + \frac{\partial}{\partial z} \hat{k} \right) \phi$$

Properties

$$(i) \nabla (C\phi) = C(\nabla \phi) \quad (ii) \nabla (\phi^n) = n\phi^{n-1} \nabla \phi$$

$$(iii) \nabla (\phi + \psi) = \nabla \phi + \nabla \psi \quad (iv) \nabla (\phi \psi) = \phi \nabla \psi + \psi \nabla \phi$$

$$(v) \nabla \left(\frac{\phi}{\psi} \right) = \frac{\psi \nabla \phi - \phi \nabla \psi}{(\psi)^2}$$

$$(i) \nabla f(r) = \frac{f'(r)}{r} \hat{r}$$

$$(ii) \nabla r = \hat{r}$$

$$(iii) \nabla \left(\frac{1}{r} \right) = -\frac{\hat{r}}{r^2}$$

$$(iv) \nabla r^n = n r^{n-2} \hat{r}$$

$\nabla \phi \cdot \hat{a}$ is called the directional derivative of ϕ in the direction $\hat{a}$.

$\Rightarrow \nabla \cdot \mathbf{A}$ is a divergence of a vector point function

$\nabla \cdot \mathbf{A}$ is scalar quantity then

$$\nabla \cdot \mathbf{A} \neq \mathbf{A} \cdot \nabla$$

$\Rightarrow$ If $\mathbf{A}$ is a constant vector then $\nabla \cdot \mathbf{A} = 0$