

vector triple product

$$A \times (B \times C) = (A \cdot C)B - (A \cdot B)C$$

$$(A \times B) \times C = (A \cdot C)B - (B \cdot C)A$$

$$A \times (B \times C) \neq (A \times B) \times C$$

$$(A \times B) \cdot (C \times D) = (A \cdot C)(B \cdot D) - (A \cdot D)(B \cdot C)$$

$$(A \times B) \times (C \times D) = (A \cdot B \times D)C - (A \cdot B \times C)D$$

linear combination

A and $B \in V$, m and n

are two scalar

$mA + nB$ is called linear combination

collinear vectors

Two vectors $\vec{A}$ and $\vec{B}$ are said to be collinear if they are parallel to the same straight line.

coplanar vectors

Three vectors A , B and C are said to be coplanar if they are parallel to the same plane.

• $|\vec{A} \cdot \vec{B}| = |\vec{A}| |\vec{B}|$ only when $\vec{A}$ and $\vec{B}$ are parallel (i.e. collinear)

• $(\vec{A} \times \vec{B})^2 = |\vec{A}|^2 |\vec{B}|^2 - (\vec{A} \cdot \vec{B})^2$ This is known as Lagrange's identity

• $\vec{A} \times \vec{B} + \vec{B} \times \vec{C} + \vec{C} \times \vec{A} = 0$ are collinear